

**Argumentasi Matematis Siswa SMA dalam Menyelesaikan Masalah
Geometri Ruang Dimensi Tiga : Studi Fenomenologi Hermeneutik**

SKRIPSI

Diajukan untuk memenuhi sebagian syarat memperoleh gelar
Sarjana Pendidikan Matematika



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**ARGUMENTASI MATEMATIS SISWA SMA DALAM MENYELESAIKAN MASALAH GEOMETRI RUANG
DIMENSI TIGA: STUDI FENOMENOLOGI HERMENEUTIK**

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LEMBAR PENGESAHAN
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ABSTRAK

Ega Charisma (1605976). Argumentasi Matematis Siswa SMA dalam Menyelesaikan Masalah Geometri Ruang Dimensi Tiga: Studi Fenomenologi Hermeneutik.

Penelitian ini bertujuan untuk mendeskripsikan argumentasi matematis siswa dalam menyelesaikan masalah geometri ruang dimensi tiga. Penelitian ini menggunakan metode penelitian kualitatif dengan pendekatan fenomenologi hermeneutic yang melibatkan siswa SMA kelas XII sebanyak 12 orang. Argumentasi matematis siswa diidentifikasi melalui soal tes argumentasi matematis dan wawancara mendalam. Sementara materi geometri ruang dimensi tiga yang digunakan pada tes argumentasi matematis yaitu mengenai jarak dalam ruang (antar titik, titik ke garis dan titik ke bidang). Berdasarkan hasil temuan dan pembahasan dalam penelitian ini, terungkap bahwa siswa belum mampu membangun argumentasi matematisnya. Hal ini ditunjukkan dari jawaban tes argumentasi matematis siswa yang belum memuat setidaknya tiga komponen utama yaitu data, warrant dan claim secara eksplisit. Sebagian besar siswa kesulitan membangun argumentasi matematisnya terkait konsep jarak titik ke garis. Pemahaman konsep geometri yang lemah membuat siswa gagal dalam membangun argumentasi matematisnya. Selain itu, bentuk soal non rutin juga menjadi hambatan bagi siswa dalam berargumentasi matematis.

Kata kunci: argumentasi matematis, jarak dalam ruang, penalaran dan pembuktian, pemahaman matematis, siswa SMA.

ABSTRACT

Ega Charisma (1605976). *Senior High School Student's Mathematical Argumentation in Solving Three Dimensional Shape Problem : a hermeneutical phenomenology study.*

This study aim to describe student's mathematical argumentation solving three dimensional shape problem. This study used qualitative research with hermeneutical phenomenology approach involving on twelve 12th grade student in senior high school. Student's mathematical argumentation was identified through mathematical argumentation test and interview with selected participant. The mathematical argumentation focus on distance in three dimensional shape (the distance between two point, a point to a line, and a point to plane). Based on the results and discussion of the research, it was showed that most of the students lack on construct their mathematical argumentation. It was showed on their answer where student's answer do not contain at least three main component (data, warrant and claim). Most of students have trouble in construct their mathematical argumentation related to the concept of distance between a point to a line. Lack of understanding on geometry concept causes students failed to construct their mathematical argumentation. Furthermore, non routine problem also be an obstacle for student to construct a mathematical argumentation.

Keywords: distance in three dimensional shape, high school student, mathematical argumentation, mathematical understanding, reasoning and proof.

DAFTAR ISI

LEMBAR PENGESAHAN	i
PERNYATAAN KEASLIAN KARYA	ii
KATA PENGANTAR	iii
UCAPAN TERIMA KASIH.....	iv
ABSTRAK	v
ABSTRACT.....	vi
DAFTAR ISI.....	vii
DAFTAR TABEL.....	ix
DAFTAR GAMBAR	x
DAFTAR LAMPIRAN.....	xi
BAB I PENDAHULUAN	1
A. Latar Belakang	1
B. Tujuan Penelitian	8
C. Rumusan Masalah.....	8
D. Manfaat Penelitian	8
BAB II KAJIAN PUSTAKA	10
A. Argumentasi Matematis	10
B. Studi Fenomenologi Hermeneutik	16
C. Concept Image dan Concept Definition.....	17
D. Materi Geometri Ruang Dimensi Tiga	18
BAB III METODE PENELITIAN.....	21
A. Desain Penelitian	21
B. Partisipan dan Tempat Penelitian.....	22
C. Pengumpulan Data	23
D. Teknik Analisis Data.....	24
E. Keabsahan Data	26
BAB IV TEMUAN DAN PEMBAHASAN	27
A. Temuan Penelitian	28
B. Pembahasan.....	45
BAB V SIMPULAN DAN REKOMENDASI	50
A. Simpulan	50

B. Implikasi	50
C. Rekomendasi.....	51
DAFTAR PUSTAKA	52
LAMPIRAN.....	57

DAFTAR TABEL

Tabel 2. 1 Kerangka Analitis Kualitas Argumentasi Matematis.....	16
Tabel 4. 1 Hasil analisis jawaban tes argumentasi matematis	28
Tabel 4. 2 Hasil Analisis Kualitas Argumentasi Matematis Siswa.....	42
Tabel 4. 3 rekapitulasi banyaknya siswa yang berada di setiap level	43

DAFTAR GAMBAR

Gambar 1. 1 Contoh soal yang diberikan kepada siswa	4
Gambar 1. 2 Contoh jawaban yang diberikan siswa.....	4
Gambar 2. 1 Struktur Argumentasi Toulmin	13
Gambar 2. 2 Ilustrasi jarak antara dua buah bangun geometri.....	19
Gambar 2. 3 Jarak antara titik ke garis dan bidang	19
Gambar 2. 4 Ilustrasi Teorema Pythagoras	20
Gambar 4. 1 Jawaban S6 terhadap soal nomor 1a	31
Gambar 4. 2 Jawaban S1 terhadap soal nomor 1b	32
Gambar 4. 3 Jawaban S6 terhadap soal nomor 1c	33
Gambar 4. 4 Jawaban S4 terhadap soal nomor 2	34
Gambar 4. 5 Jawaban S3 terhadap soal nomor 3	35
Gambar 4. 6 Jawaban S5 terhadap soal nomor 4	36
Gambar 4. 7 Jawaban S6 terhadap soal nomor 5	38
Gambar 4. 8 Jawaban S4 terhadap soal nomor 6	40
Gambar 4. 9 Jawaban S6 terhadap soal nomor 6	40
Gambar 4. 10 Jawaban siswa level 0	43
Gambar 4. 11 Jawaban siswa Level 1	44
Gambar 4. 12 Jawaban siswa level 2	44

DAFTAR LAMPIRAN

Lampiran 1 : Kisi-kisi Instrumen Tes	57
Lampiran 2: Instrumen tes	64
Lampiran 3: Pedoman Wawancara	66
Lampiran 4 : Transkrip Wawancara.....	73
Lampiran 5: Riwayat Hidup Penulis	90

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