

STATEMENT OF ORIGINALITY

This is to certify that to the best of my knowledge, the content dissertation entitled **“Mathematical Abstraction of Pre-Service Mathematics Teachers in Learning Non-Conventional Mathematics Concept”** is my own work. This dissertation has not been submitted for any degree or other purposes. I certify that the intellectual content of this dissertation is the product of my own work and that all the assistance received in preparing this thesis and sources have been acknowledged. I am not plagiarizing or citing in ways that are inconsistent with the ethics of science prevailing in scientific societies. On this statement, I am ready to bear the risks/sanctions if in the future found a violation of scientific ethics or there are claims from others to the authenticity of this work of mine.

Bandung, January 2018

Farida Nurhasanah

PERNYATAAN

Dengan ini saya menyatakan bahwa disertasi dengan judul “**Mathematical Abstraction of Pre-Service Mathematics Teachers in Learning Non-Conventional Mathematics Concept**” ini beserta seluruh isinya adalah benar-benar karya saya sendiri. Saya tidak melakukan penjiplakan atau pengutipan dengan cara-cara yang tidak sesuai dengan etika ilmu yang berlaku dalam masyarakat keilmuan. Atas pernyataan ini, saya siap menanggung resiko/sanksi apabila dikemudian hari ditemukan adanya pelanggaran etika keilmuan atau ada klaim dari pihak lain terhadap keaslian karya saya ini.

Bandung, January 2018

Yang membuat pernyataan

Farida Nurhasanah

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This dissertation has led to several conferences, journal paper, and chapter book which are already published or in the process of publication. Some of the papers are prepared in collaboration with Prof. Yaya S. Kusumah, M.Sc., Ph.D., Prof. Jozua Sabandar, M.A., Ph.D. and Prof. Didi Suryadi, M.Ed. Two papers are prepared in collaboration with Prof. Yaya S. Kusumah, M.Sc., Ph.D., only. In addition, a paper published together with Prof. Turmudi, M.Ed., Ph.D. and Eys Sudihartinih, M.Pd., and a paper published in collaboration with Ahmad Saddam Siregar, S.Si. I hereby would like to acknowledge the authorship and contribution of these academics to the relevant sections of this dissertation in which the contents of the jointly produced papers are used. A list of the papers stemming from this study is presented below.

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