

**PEMECAHAN MASALAH MATEMATIS NON RUTIN
PADA TOPIK TEOREMA PYTHAGORAS
(STUDI TRANSPOSISIONAL)**

SKRIPSI

diajukan untuk memenuhi sebagian syarat untuk memperoleh gelar Sarjana

Pendidikan Matematika



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UNIVERSITAS PENDIDIKAN INDONESIA
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2019**

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Sarjana Pendidikan pada Program Studi Pendidikan Matematika, Fakultas
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